

# Probing dynamical heterogeneity by XPCS

*LCVN Montpellier*

Luca Cipelletti

Agnès Duri

Estelle Pitard

Laurence Ramos

*Université de Fribourg*

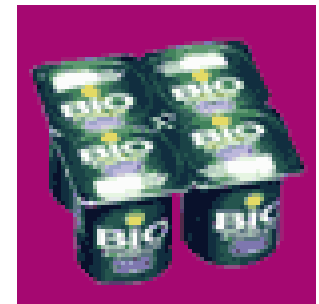
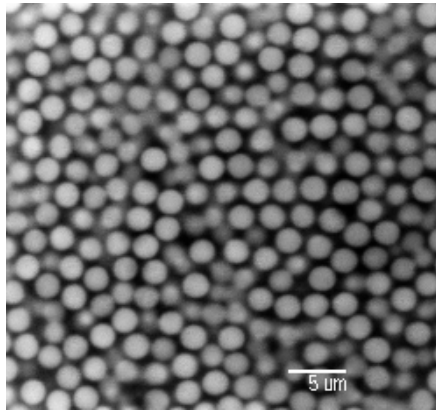
Véronique Trappe

Hugo Bissig

*ESRF*

Aymeric Robert

# Soft glassy/jammed materials

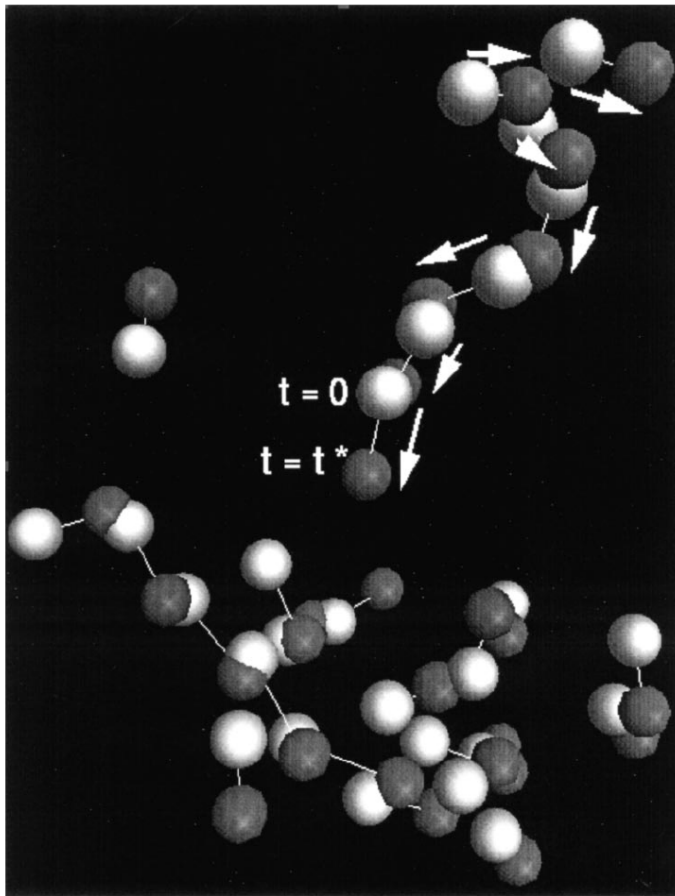


# Overview

- Slow dynamics and dynamical heterogeneities in soft glasses
- How to probe DH: Time Resolved Correlation (TRC)
- XPCS measurement of DH in a gel system
- Bringing together Imaging and Scattering

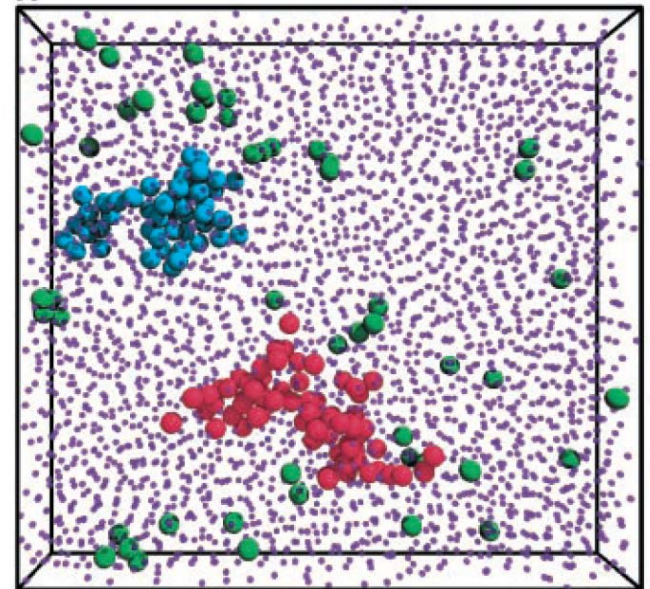
# Dynamical Heterogeneity

## LJ supercooled fluid



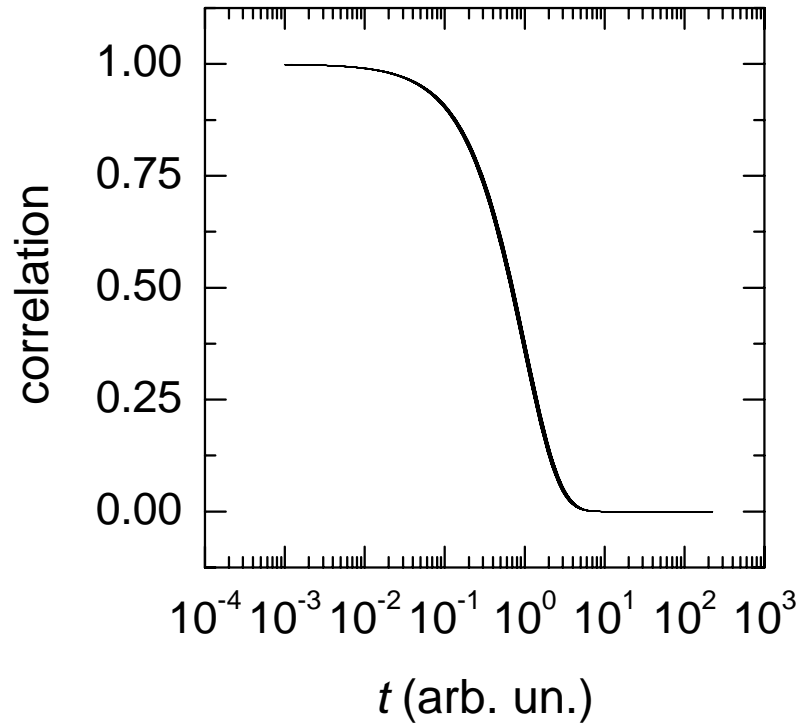
Donati et al. PRL 98

## Supercooled colloidal HS



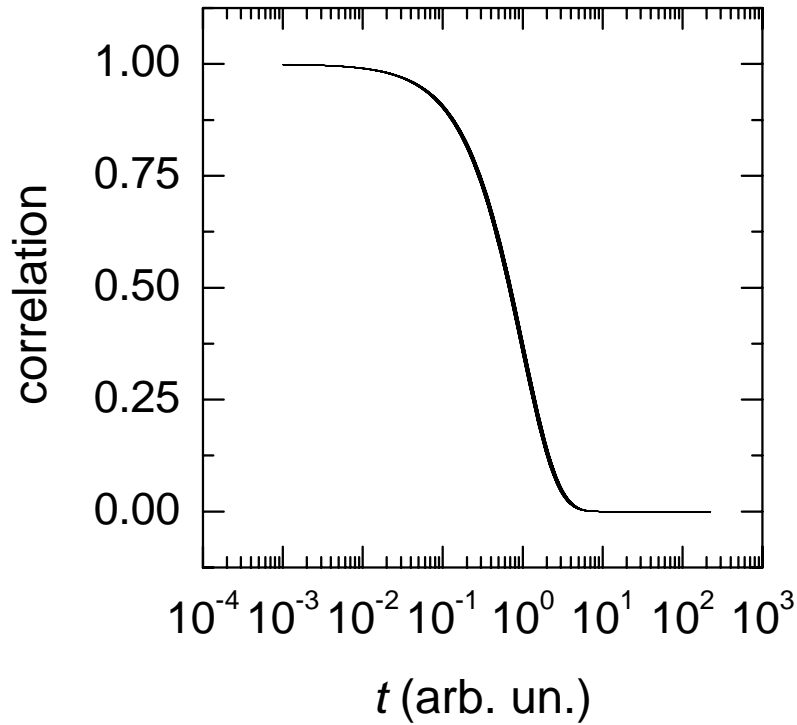
Weeks et al. Science 2000

# Temporally heterogeneous dynamics

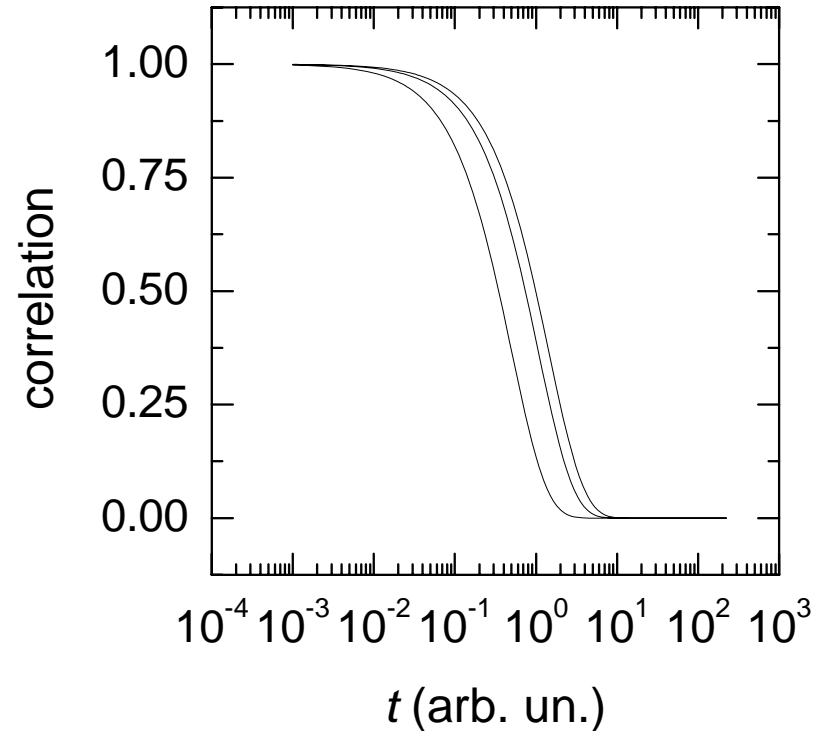


**homogeneous**

# Temporally heterogeneous dynamics

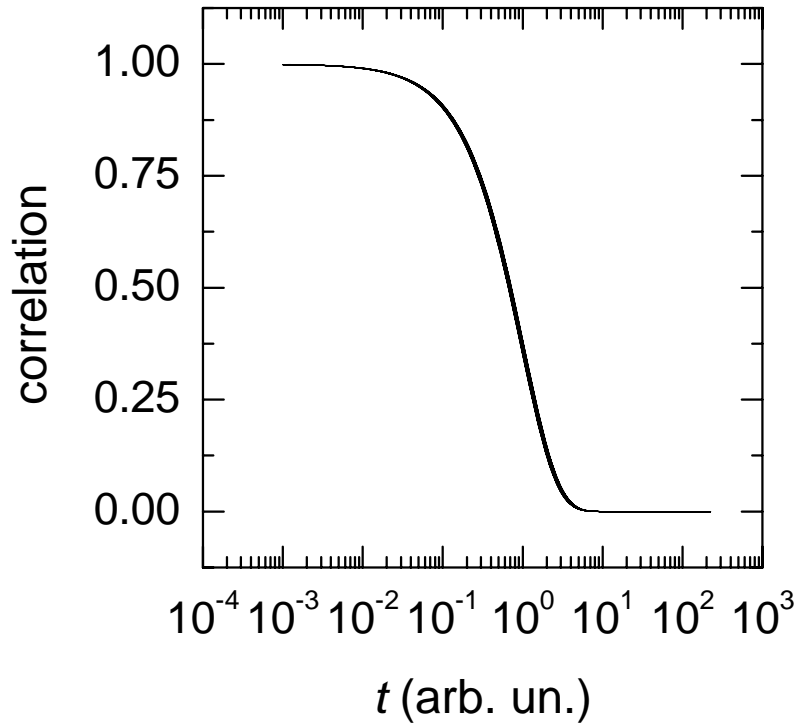


**homogeneous**

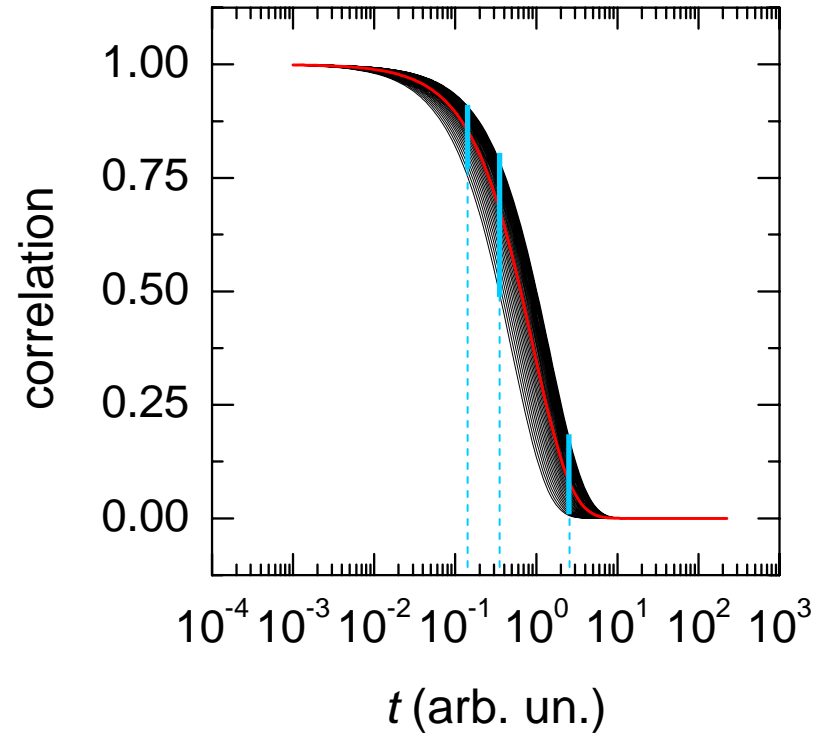


**heterogeneous**

# Temporally heterogeneous dynamics



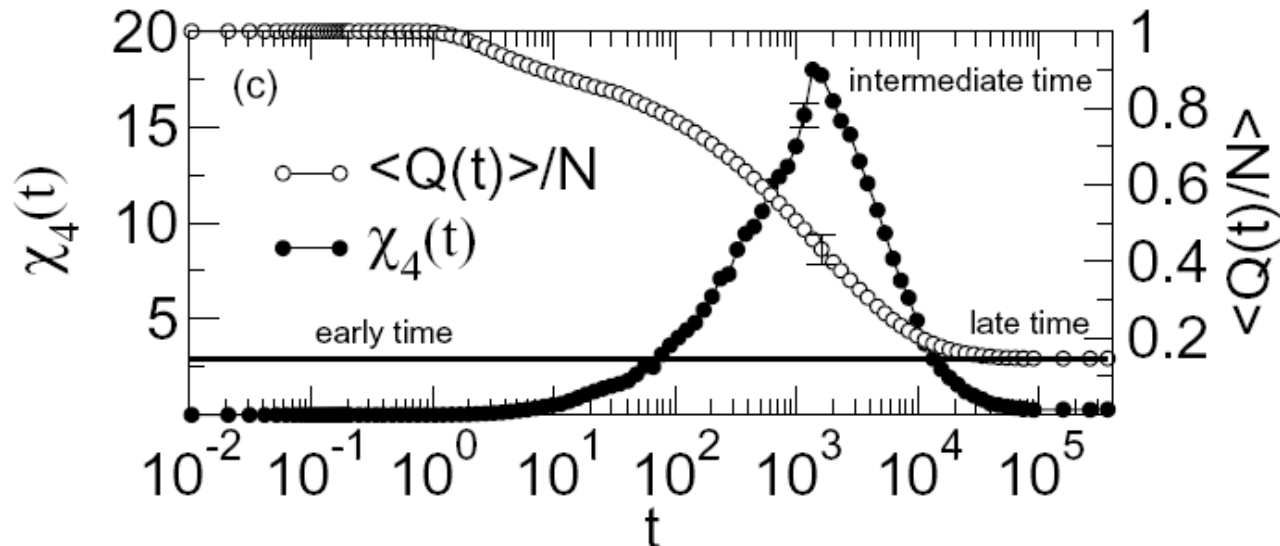
**homogeneous**



**heterogeneous**

# Dynamical susceptibility in glassy systems

## Supercooled liquid (Lennard-Jones)

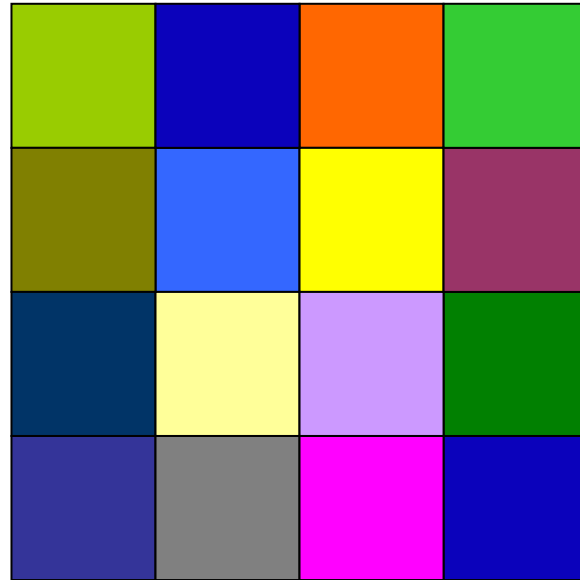


Lacevic et al., PRE 2002

$$\chi_4 \sim \text{var}[Q(t)]$$



# Dynamical susceptibility in glassy systems

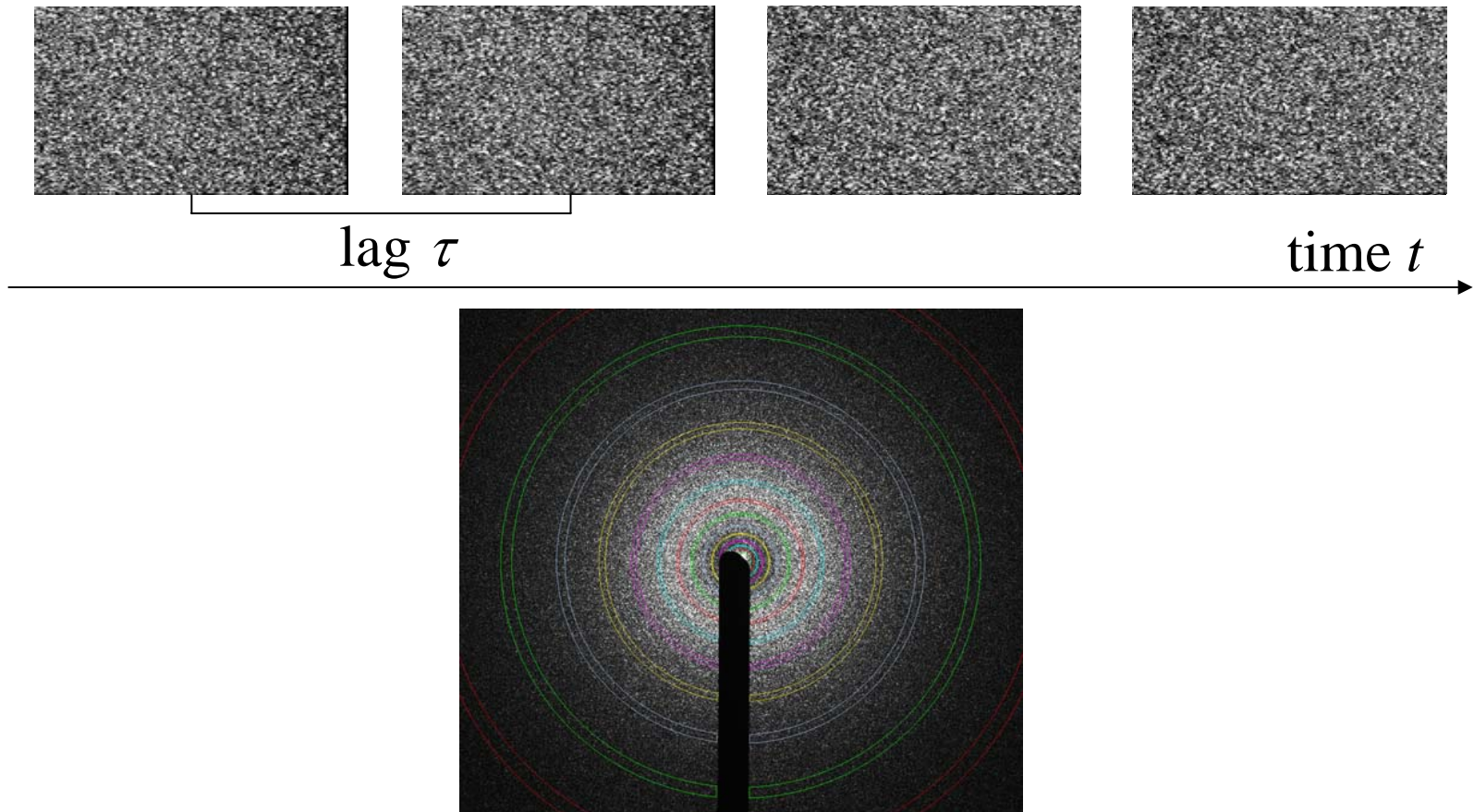


$N_{\text{blob}}$  regions

$$\chi_4 \sim \text{var}[Q(t)] \sim 1/N_{\text{blob}}$$

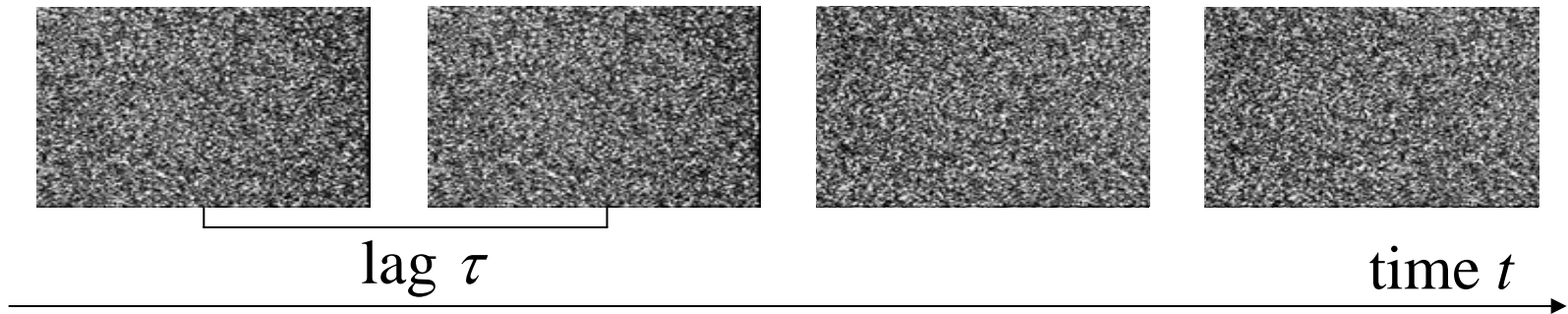
# Fluctuations of the dynamics: Time Resolved Correlation

[Cipelletti et al. J. Phys:Condens. Matter 2003],  
[Duri et al. PRE 2006]



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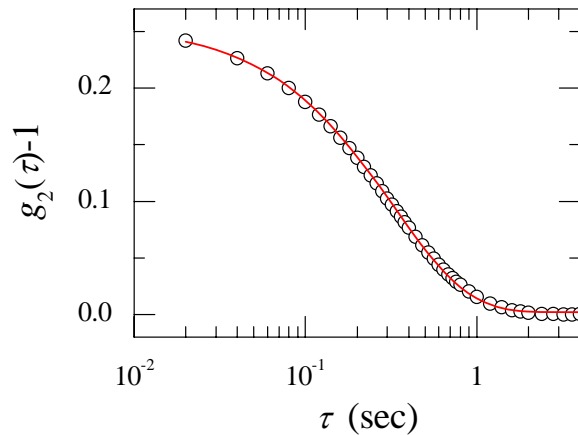


**degree of correlation**  $c_I(t, \tau) = \frac{\langle I_p(t) I_p(t + \tau) \rangle_p}{\langle I_p(t) \rangle_p \langle I_p(t + \tau) \rangle_p} - 1$

$$\text{degree of correlation } c_I(t, \tau) = \frac{\langle I_p(t) I_p(t + \tau) \rangle_p}{\langle I_p(t) \rangle_p \langle I_p(t + \tau) \rangle_p} - 1$$

Average over  $t$  ↓

intensity correlation  
function  $g_2(\tau) - 1$



$g_2(\tau) - 1$  → Average dynamics

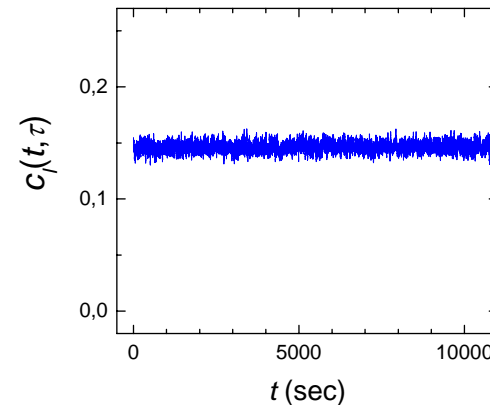
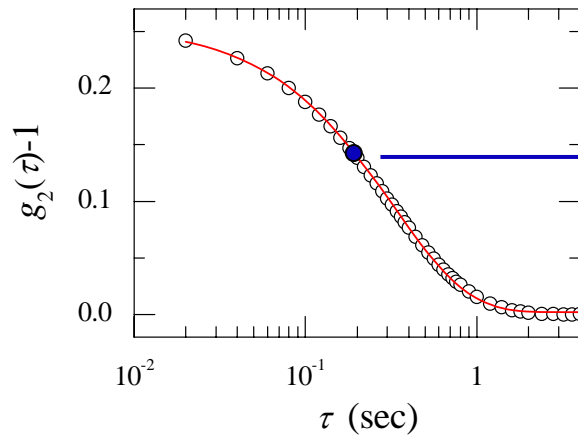
**degree of correlation**  $c_I(t, \tau) = \frac{\langle I_p(t) I_p(t + \tau) \rangle_p}{\langle I_p(t) \rangle_p \langle I_p(t + \tau) \rangle_p} - 1$

Average over  $t$  ↓

intensity correlation  
function  $g_2(\tau) - 1$

fixed  $\tau$ , vs.  $t$  ↓

**fluctuations** of the dynamics



$g_2(\tau) - 1$  → Average dynamics

**Brownian particles**

**degree of correlation**  $c_I(t_w, \tau) = \frac{\langle I_p(t_w) I_p(t_w + \tau) \rangle_p}{\langle I_p(t_w) \rangle_p \langle I_p(t_w + \tau) \rangle_p} - 1$

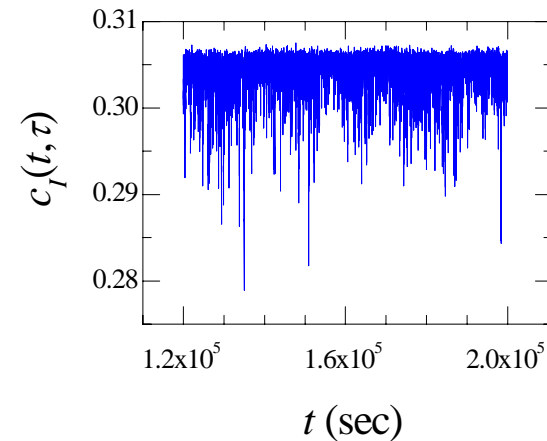
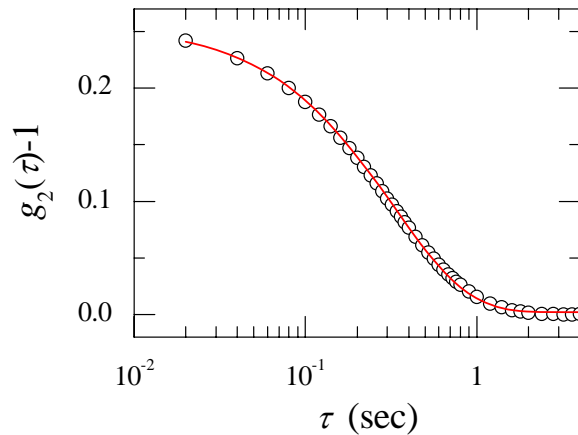
Average over  $t_w$  ↓

intensity correlation  
function  $g_2(\tau) - 1$



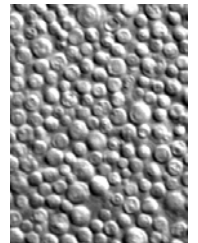
fixed  $\tau$ , vs.  $t_w$

**fluctuations** of the dynamics



$g_2(\tau) - 1$  → Average dynamics

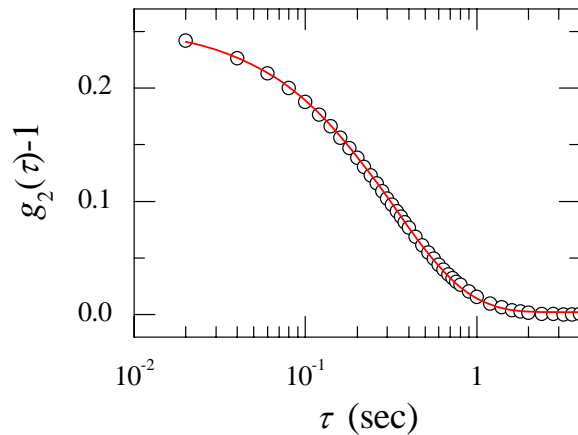
**Onion gel**



**degree of correlation**  $c_I(t_w, \tau) = \frac{\langle I_p(t_w) I_p(t_w + \tau) \rangle_p}{\langle I_p(t_w) \rangle_p \langle I_p(t_w + \tau) \rangle_p} - 1$

Average over  $t_w$  ↓

intensity correlation  
function  $g_2(\tau) - 1$

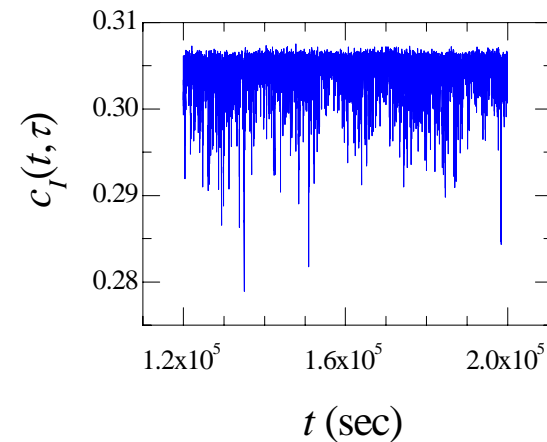


$g_2(\tau) - 1$  → Average dynamics



fixed  $\tau$ , vs.  $t_w$

**fluctuations** of the dynamics

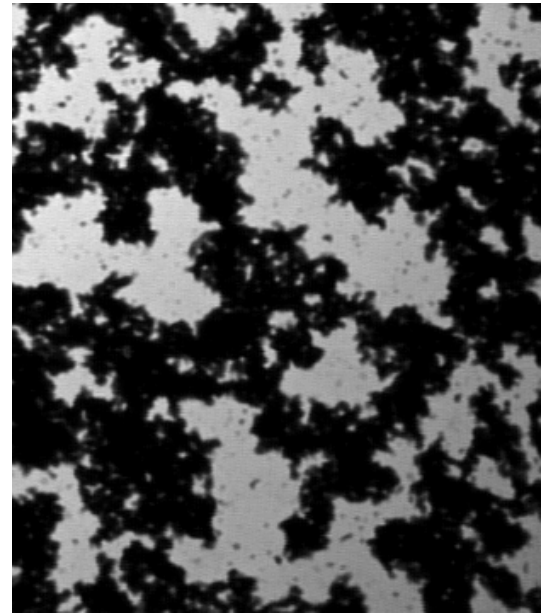


$\text{var}(c_I) \rightarrow \chi_4$

# XPCS measurements of the dynamics of a Carbon Black gel

[Trappe et al., PRE 2007]

- Particle size  $R = 180$  nm
- Suspended in mineral oil at  $\phi = 6\%$
- Attractive interactions controlled by adding a dispersant:  
 $U \sim 12 k_B T$  and  $U \sim 30 k_B T$
- XPCS @ ID10 Troika beamline (ESRF)







# Average dynamics

Fit :  $A \exp[-(\tau/\tau_i)^p]$

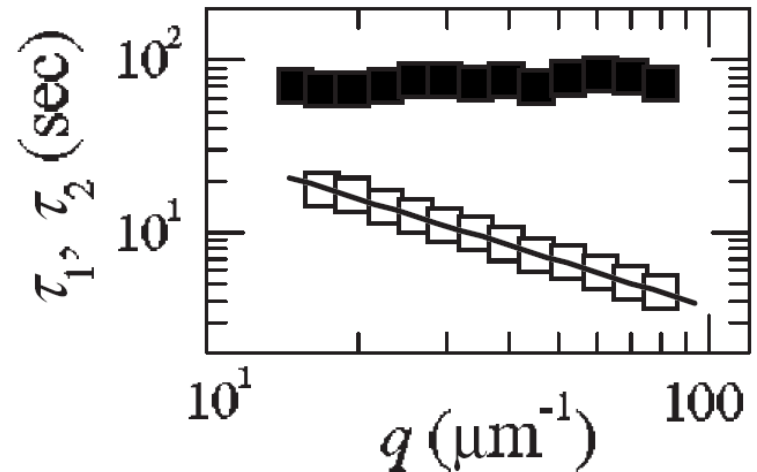
**Initial decay:**  $\tau_1 \sim q^{-0.91}$ ,  $p = 1.2$

Stress-relaxation driven dynamics

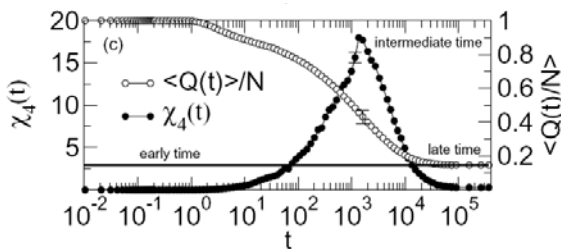
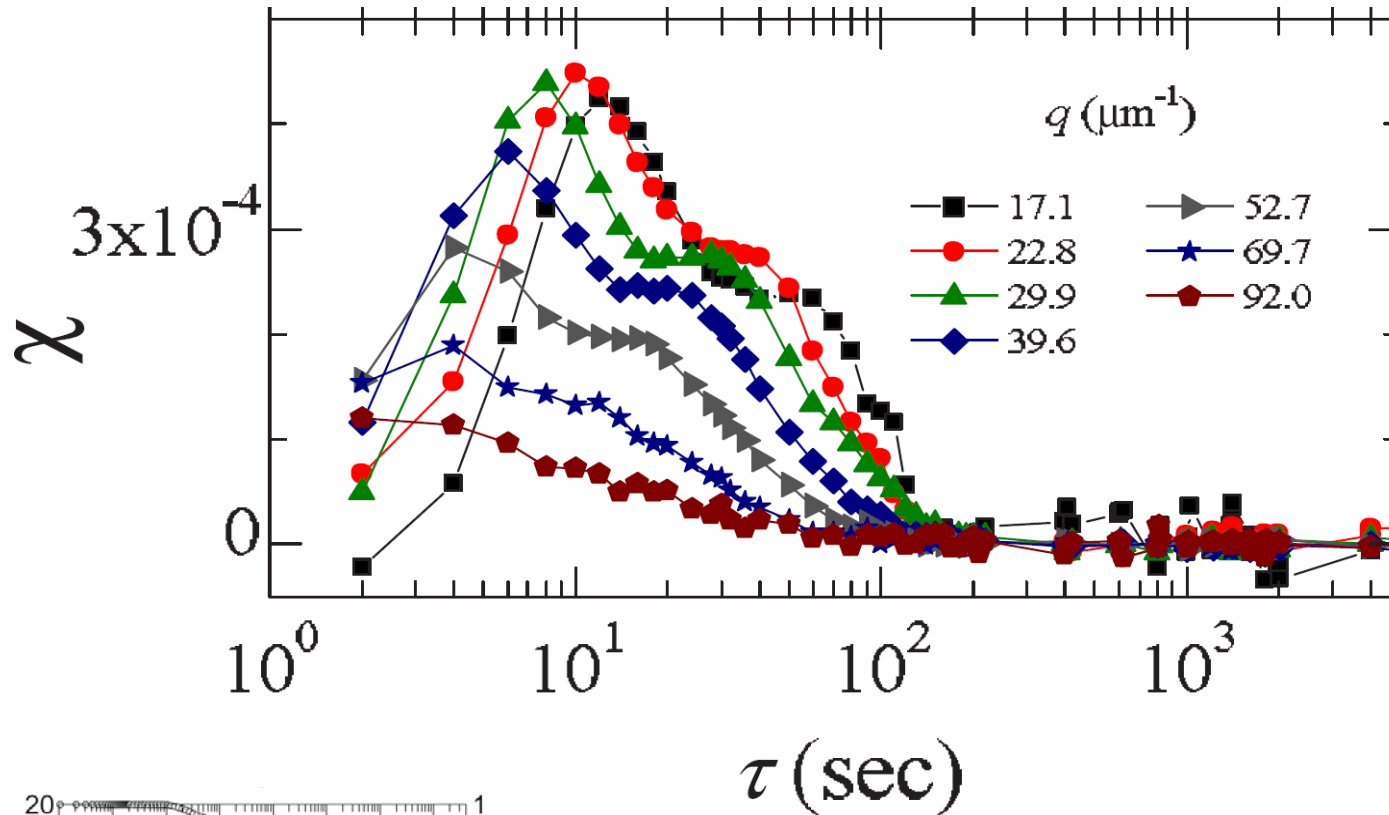
**Final decay:**  $\tau_2 \sim q^0$ ,  $p = 1$

Bond breaking?

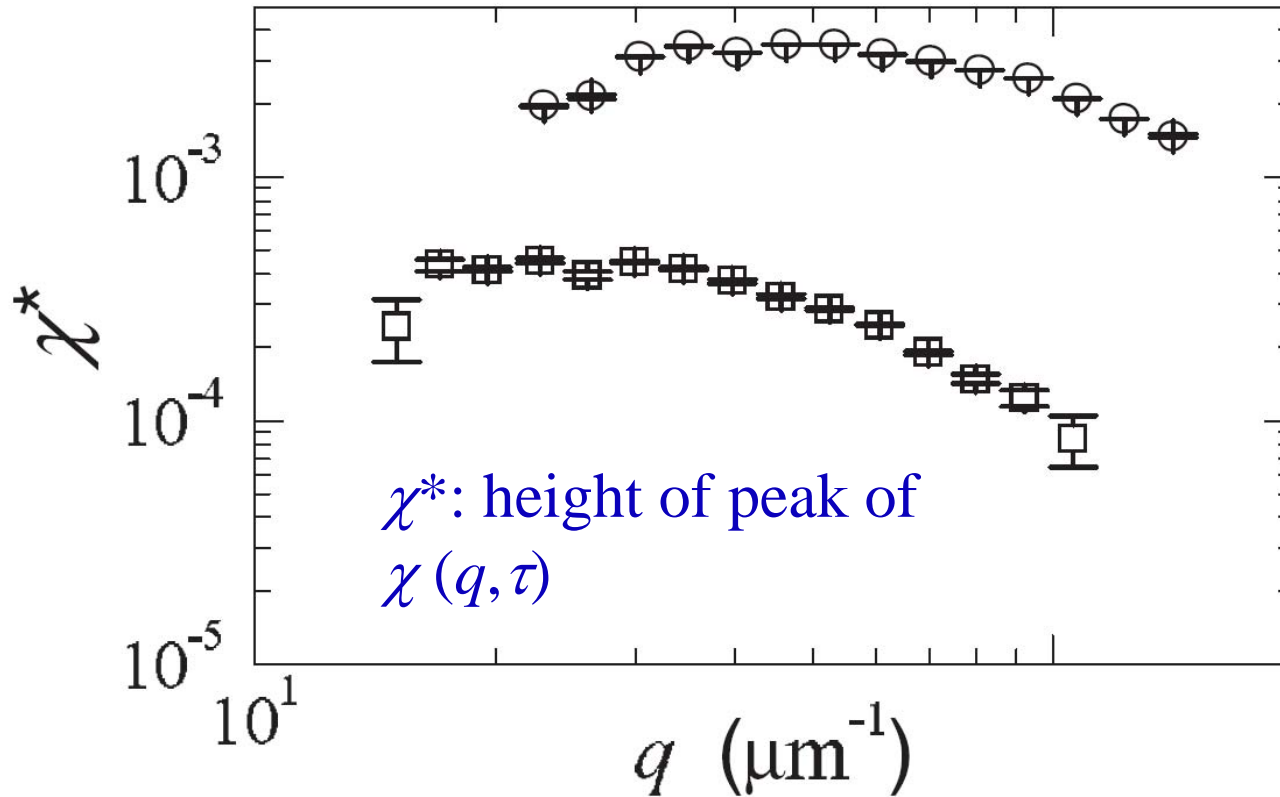
(no final decay for the gel with  $U \sim 30 k_B T$ )



# Fluctuations of the dynamics: dynamical susceptibility $\chi = \text{var}[c_I]$



# $q$ -dependence of the amplitude of $\chi$

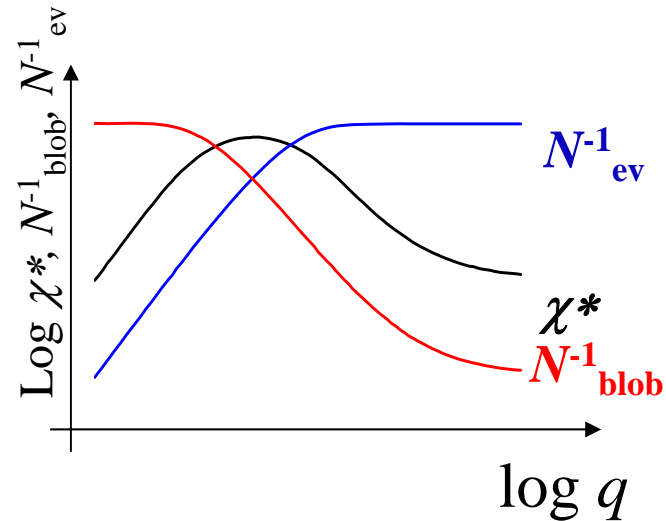


**Non-monotonic behavior** (see also Charbonneau & Reichman, PRL 2007)

# $q$ -dependence of $\chi^*$ : a simple argument

$\chi^* \sim (\text{\# rearrangements in the scattering volume needed to decorrelate the scattered light})^{-1}$

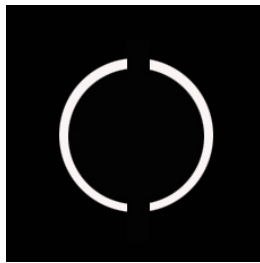
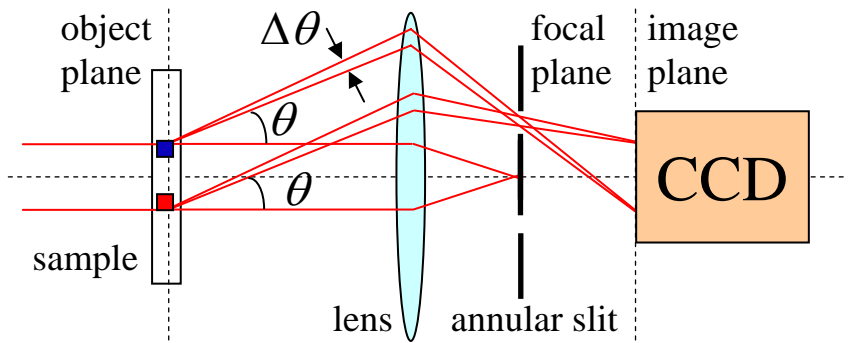
$$\chi^* \sim (N_{\text{blob}} N_{\text{ev}})^{-1}$$



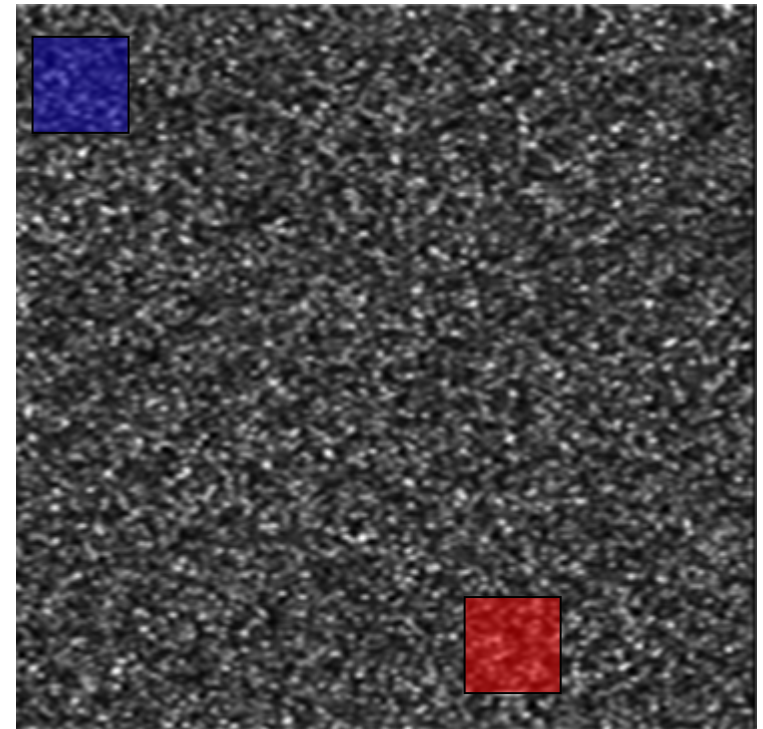
$N_{\text{blob}}$ ,  $N_{\text{ev}}$  depend on  $q$ ,  $t_w$ ,  $\varphi$ , ...

# Photon Correlation Imaging (PCIm)

[Duri et al., PRL 2009]



$$\theta = 6.4^\circ \longrightarrow q = 1 \mu\text{m}^{-1}.$$



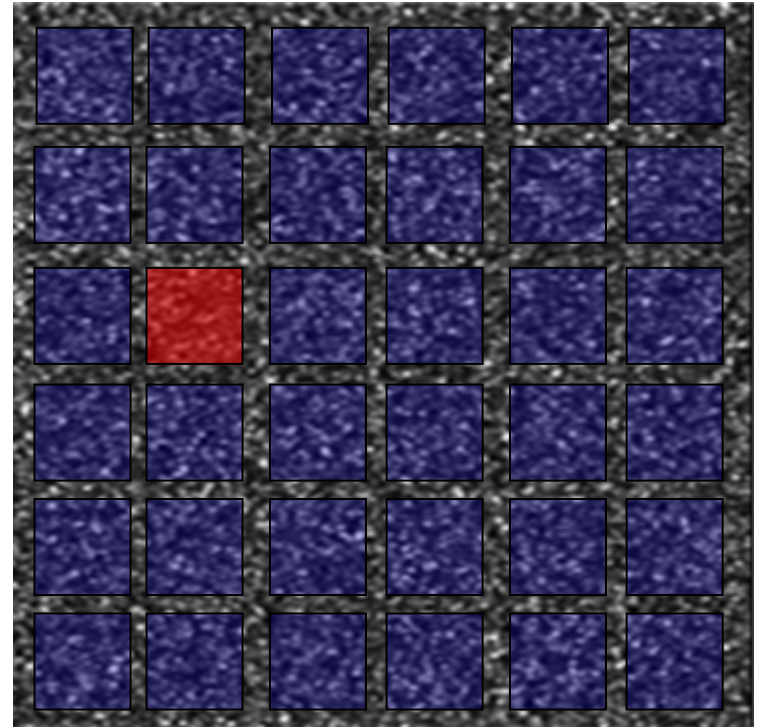
2.3 mm

# Local, instantaneous dynamics: $c_I(t, \tau, \mathbf{r})$

$$c_I(t, \tau, \mathbf{r}) = \frac{\langle I_p(t) I_p(t + \tau) \rangle_{p(\mathbf{r})}}{\langle I_p(t) \rangle_p \langle I_p(t + \tau) \rangle_{p(\mathbf{r})}} - 1$$

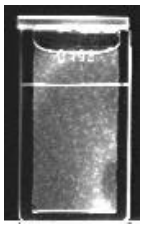
Note:  $\langle \langle c_I(t, \tau, \mathbf{r}) \rangle_t \rangle_{\mathbf{r}} = g_2(\tau) - 1$

$[g_2(\tau) - 1]^{1/2} \sim$  dynamic structure factor

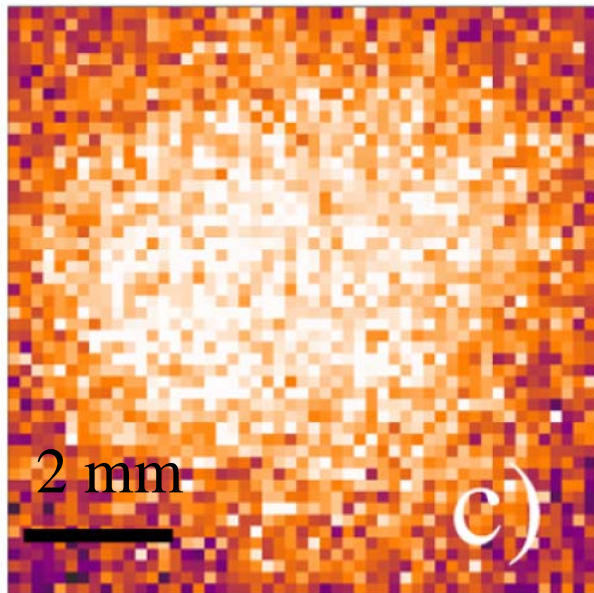


2.3 mm

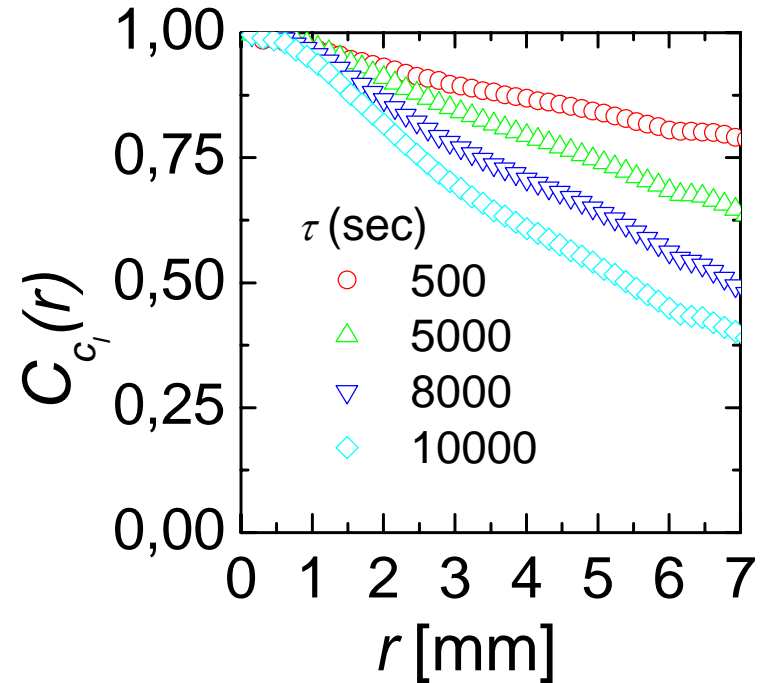
# Strongly attractive colloidal gel (PS)



Dynamical activity map



$\tau = 500$  sec  
( $\sim \tau_r/10$ )



**Ultra long-ranged correlations!**  
(particle size: 20 nm  
cluster size:  $\sim 20 \mu\text{m}$ )



# Conclusions

- Scattering techniques can measure **instantaneous/spatially resolved dynamics**
- Slow dynamics of systems jammed/close to jamming are **heterogeneous**
- Spatial correlations can be **very long ranged!**
- A **PCI** setup for **XPCS?**

# Thanks to...

## *People:*

D. Weitz

J. P. Garrahan

J. P. Bouchaud

G. Biroli

## *Funding:*

CNES

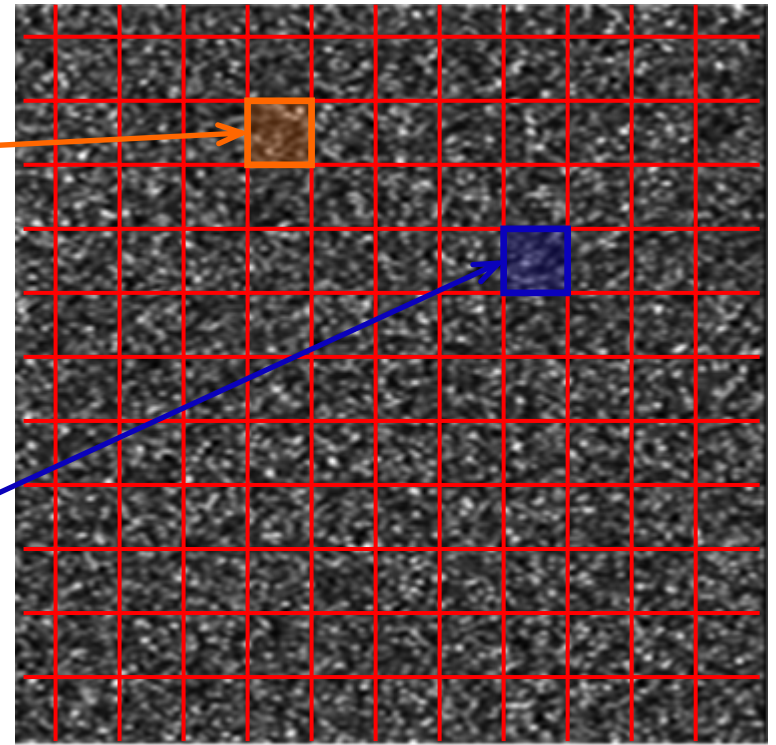
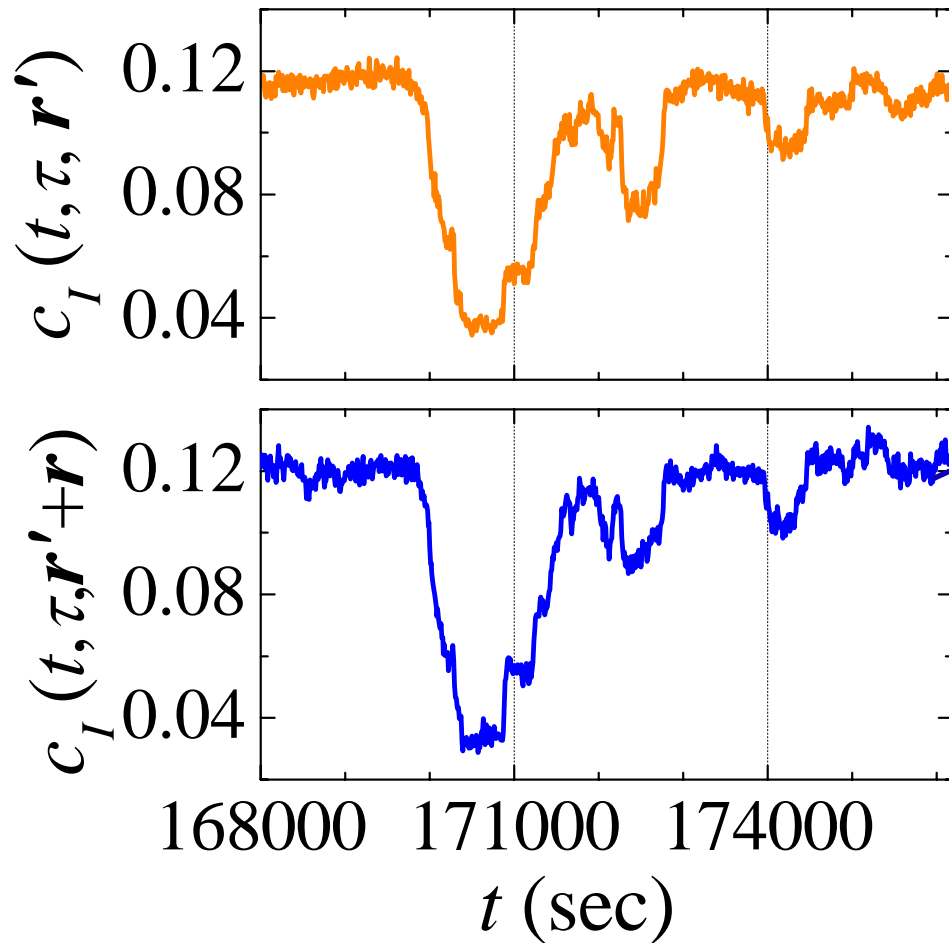
CNRS (PICS, mi-lourd)

MR (ACI Jeunes Chercheurs)

EU (SoftComp, Arrested Matter)

IUF

# Size of a rearrangement: space-resolved TRC



2.3 mm